

Arithmetic in the developing brain:

A review of brain imaging studies

Lien Peters and Bert De Smedt

Parenting and Special Education Research Unit,

Faculty of Psychology and Educational Sciences

KU Leuven, University of Leuven, Belgium

Corresponding author:

Bert De Smedt, Parenting & Special Education Research Unit, University of Leuven

Leopold Vanderkelenstraat 32, box 3765, B-3000 Leuven, BELGIUM

Tel. +32 16 32 57 05; Fax. +32 16 32 59 33

e-mail: Bert.DeSmedt@ppw.kuleuven.be

Abstract

Brain imaging studies on academic achievement offer an exciting window on experience-dependent cortical plasticity, as they allow us to understand how developing brains change when children acquire culturally transmitted skills. This contribution focuses on the learning of arithmetic, which is quintessential to mathematical development. The nascent body of brain imaging studies reveals that arithmetic recruits a large set of interconnected areas, including prefrontal, posterior parietal, occipito-temporal and hippocampal areas. This network undergoes developmental changes in its function, connectivity and structure, which are not yet fully understood. This network only partially overlaps with what has been found in adults, and clear differences are observed in the recruitment of the hippocampus, which are related to the development of arithmetic fact retrieval. Despite these emerging trends, the literature remains scattered, particularly in the context of atypical development. Acknowledging the distributed nature of the arithmetic network, future studies should focus on connectivity and analytic approaches that investigate patterns of brain activity, coupled with a careful design of the arithmetic tasks and assessments of arithmetic strategies. Such studies will produce a more comprehensive understanding of how the arithmetical brain unfolds, how it changes over time, and how it is impaired in atypical development.

1. Introduction

Brain imaging studies on academic achievement offer an exciting window on experience-dependent cortical plasticity, as they allow us to understand how developing brains change when children acquire culturally transmitted skills, such as reading or arithmetic (Dehaene & Cohen, 2007). This contribution focuses on the learning of arithmetic, i.e. the ability to add, subtract, multiply and divide symbolic whole numbers. This skill constitutes a major element of the mathematics curriculum in primary school (National Mathematics Advisory Panel, 2008) and has a quintessential role in mathematical development (Kilpatrick et al., 2001) for children around the globe. There are large individual differences at the behavioral (Dowker, 2005; Vanbinst & De Smedt, 2016, for a review) and neural levels in this basic competence, even in adulthood (Grabner et al., 2007). On the other hand, persistent deficits in learning arithmetic constitute the hallmark of dyscalculia, a specific neurodevelopmental learning disorder that is characterized by life-long difficulties in calculation that are not merely explained by intellectual disabilities, uncorrected sensory problems, mental or neurological disorders or inadequate instruction (DSM-V, American Psychological Association, 2013).

This contribution starts with a succinct discussion of children's arithmetic development and its supporting cognitive competencies, as well as a brief summary of brain imaging studies in adults. These two sections are short and only provide a lens through which we subsequently discuss the available neural data in children. We systematically review functional brain imaging studies in typically and atypically developing populations and provide an overview of connectivity studies. We also discuss structural brain imaging data that have correlated variability in arithmetic performance with individual differences in white and grey matter properties. This review ends with challenges and outstanding issues that should be considered in future studies.

2. Arithmetic development is characterized by strategy change

Decades of cognitive developmental research have investigated the acquisition of arithmetic and this development involves a change in the mix of strategies that are used to calculate the answer to a particular problem (Geary, 2011; Jordan et al., 2003; Siegler, 1996, for reviews). Already before the start of formal schooling, children use counting to solve simple sums. These counting strategies are initially executed with additional support, such as manipulatives or fingers, yet progressively, children execute these strategies without external aids (verbal counting). The efficiency of these counting strategies increases rapidly with grade, where children move from counting all sets in their entirety to counting from the first (counting-on) or larger (counting-on-larger) number (Geary et al., 1992). The repeated use of these counting routines allows children to develop associations between problems and their answers, arithmetic facts, which are stored in long-term memory. The acquisition of these facts is important because fact retrieval is more efficient and it consumes less working memory than the more cognitively demanding and error-prone procedures, such as counting. The availability of arithmetic facts also allows children to use these facts to decompose problems into smaller problems, such as $7 + 8 =$, $7 + 3 = 10$, $10 + 5 = 15$. These decomposition strategies usually occur in problems with larger numbers (typically when they cross 10) and, evidently, in multi-digit calculations. They are used more often during addition and subtraction – albeit more frequently in subtraction than in addition (Barrouillet et al., 2008) - but they are much less used in multiplication, in which fact retrieval is the most dominant strategy from an early point on in development, i.e. second grade (Imbo & Vandierendonck, 2007; Lemaire & Siegler, 1995). This is because

multiplications are typically learned by extensive (rote) training of the multiplication tables rather than by decomposing the problem in its smaller sub-parts, as is often the case in subtraction. On the other hand, multiplication and addition are commutative operations (e.g. $6 \times 4 = 4 \times 6$), in contrast to division and subtraction. This commutativity might facilitate the formation of problem-answer associations in long-term memory for multiplication and addition, for which reason they are more often solved via fact retrieval. Surprisingly little is known about the development of division, but the available evidence suggests that its strategies follow a somewhat different developmental trajectory (Robinson et al., 2006). Because, to the best of our knowledge, there are no developmental brain imaging studies on division, this operation is not considered further.

The development of these strategies is not an abrupt shift from one strategy to the other but rather a change in the frequency distributions of strategies children use, the so-called overlapping waves theory (Siegler, 1996). This theory posits that strategies remain available over development, even in adulthood (LeFevre et al., 1996), but that the frequency in their use changes at different time points, with the more efficient strategies, such as fact retrieval, becoming more dominant. This change is also accompanied by changes in brain activity, as we will review below. Interestingly, similar strategy shifts have been documented in the learning of other academic domains (Siegler, 1996). For example, in word reading, children move towards an increased reliance on efficient orthographic direct recognition coupled with a decreased reliance on phonological decoding (Schlagger & McCandliss, 2007) and the changes in brain structure and function that accompany this (a)typical development have been described (Eden et al., 2016 for a review).

The acquisition of these strategies is supported by additional cognitive competencies that can be characterized as domain-specific, i.e. specifically relevant for learning arithmetic but not for other academic skills, or domain-general, i.e. relevant to learning other academic skills, such as reading, or to learning in general, such as working memory (e.g., Geary & Moore, 2016; Vanbinst & De Smedt, 2016 for a review). A detailed review of these factors is beyond the scope of this paper, but we briefly highlight some of them to frame the subsequent brain imaging data.

One domain-specific factor that has received a lot of attention in studies on individual differences in arithmetic is the ability to process numerical magnitudes (De Smedt et al., 2013; Schneider et al., 2016, for a meta-analysis). It turns out that specifically the ability to process symbolic numerical magnitudes is uniquely related, cross-sectionally (Vanbinst et al., 2012) and predictively (Vanbinst et al., 2016; Vanbinst, Ceulemans, et al., 2015; Vanbinst, Ghequière, & De Smedt, 2015), to children's arithmetic strategy use and their increasing reliance on fact retrieval. These associations are not limited to addition and subtraction, but are also observed in multiplication (De Visscher & Noël, 2016; Schleepe et al., 2016).

The fact that symbolic numerical magnitude processing is key to arithmetic development has been connected to the observation that the intraparietal sulcus (IPS) is consistently active whenever people calculate. Indeed, increases in IPS-activity during calculation have been frequently interpreted to reflect the processing of numerical magnitude (e.g., Ansari, 2008; Menon, 2015). On the other hand, atypical IPS structure (e.g., Isaacs et al., 2001) or function (e.g., Price et al., 2007) has been suggested to represent the neural origin of dyscalculia, and these are assumed to reflect poor numerical magnitude processing, which is seen as the core deficit in dyscalculia that cascades into impairments in arithmetic (e.g., De Smedt et al., 2013; Rubinsten & Henik, 2006). This recent

emphasis on particularly symbolic numerical magnitude processing has somewhat mistakenly narrowed down the attention to the IPS in studying brain activity during arithmetic (see Fias et al., 2013; Menon, 2015, for critical analyses). Indeed, arithmetic tasks typically recruit a large set of bilateral regions including the dorsolateral (DLPFC) and ventrolateral prefrontal cortex (VLPFC), anterior cingulate (ACC), temporo-parietal cortex (angular (AG) and supramarginal gyri (SMG)), the occipito-ventral cortex (including fusiform gyrus (FG)) and the medial temporal lobe (Arsalidou & Taylor, 2011; Menon, 2016). This suggests the involvement of domain-general processes as well, and behavioral studies have already confirmed that working memory (Peng et al., 2016), executive functions (Bull & Lee, 2014), interference control (De Visscher et al., 2015), phonological processing (De Smedt et al., 2010; Hecht et al., 2001) and retrieval from long-term memory (Garnett & Fleischner, 1983) are uniquely related to individual differences in arithmetic. In all, these data suggest that both domain-specific and domain-general factors should be considered when studying brain activity during arithmetic and that such analysis should not be restricted to the parietal cortex.

We end this section with a brief discussion on how arithmetic strategies are measured (De Smedt, 2016, for a more elaborate discussion). In behavioral research, this mix of strategies has typically been measured through verbal report data (e.g., Campbell & Xue, 2001; Imbo & Vandierendonck, 2007; Siegler, 1996) in which children have to verbally indicate on a trial-by-trial basis which strategy they used to solve the problem. Responses can be reliably and validly classified into categories (Siegler & Stern, 1998), such as *retrieval* (the child immediately knew the answer with no overt signs of calculations) or *procedures* (the child counted or decomposed the problem into smaller problems). The collection of verbal report data is quite difficult in brain imaging studies. Some adult studies have analyzed brain activity as a function of verbally reported strategy (Grabner et al., 2009; Grabner & De Smedt, 2011; Tschentscher & Hauk, 2014), but such trial-by-trial strategy data have not been reported in children. For this reason, brain imaging studies have typically used designs in which they compared brain responses of sets of problems on which the use of a particularly strategy was expected on the basis of specific characteristics of the problem, i.e. its size (De Smedt et al., 2011), complexity (Ashkenazi et al., 2012) or operation (Prado et al., 2014). This approach has been criticized (De Smedt, 2016; Siegler, 1987): Not all problems of a given type are solved by the same strategy and aggregating across problem types leads to misleading conclusions (Siegler, 1987). This is especially true for developmental research and studies in atypical populations: Children will differ in their mix of strategies for a given problem type or operation, depending on their age, education or ability level (typical vs. atypical). Therefore, verbal report data may be the most optimal way to study brain activity during arithmetic in developing populations. On a related note, electrophysiological data in adults (Grabner & De Smedt, 2011) have shown that such verbal report data correlate with differences in brain activity, which are not revealed when focusing on problem size or operation alone.

3. Adult brain imaging data

The vast majority of research on the neural correlates of arithmetic has been performed in adults. Studies in adults date back to the description of patients with lesions in the (left) parietal cortex (Gerstmann, 1940; Henschen, 1919) that were accompanied by difficulties in performing arithmetic. Summarizing a series of patients, Dehaene and Cohen (1995) postulated the triple-code model, which included three numerical codes that support different arithmetical processes, including arithmetic fact retrieval (verbal code, located in the left AG) and the execution of (magnitude-based)

procedures (magnitude code, situated in the IPS). Conventional non-invasive fMRI methods subsequently allowed to further delineate this arithmetic network, revealing repeatedly that a large, whole-brain network is active when adults perform arithmetic (Arsalidou & Taylor, 2011; Menon, 2015). This network includes the bilateral posterior parietal cortex, inferior and superior prefrontal cortex (PFC), and occipito-temporal regions. Activity in this network is modulated by the arithmetic operation (Rosenberg-Lee et al., 2011), strategy use (Grabner et al., 2009; Tschentscher & Hauk, 2014), expertise (Grabner et al., 2007) and training (Zamarian et al., 2009).

Consistent across these data is the activation of the bilateral IPS during arithmetic, potentially reflecting the role of numerical magnitude processing during calculation (Arsalidou & Taylor, 2011). It also has been suggested that activity in this area is higher for subtractions, large problems and during the execution of procedural strategies. Activity in the temporo-parietal cortex (AG and SMG), has been typically associated with the retrieval of arithmetic facts from long-term memory. Increases in brain activity in this area are usually observed in multiplication and correlate with mathematical expertise (Grabner et al., 2007). Originally, this temporo-parietal activity was thought to reflect the involvement of phonological processes in fact retrieval and multiplication. This interpretation has been questioned (Menon, 2015) and recent data by De Visscher et al. (2015) suggest that it rather reflects the automatic mapping between an arithmetic problem and its answer in long-term memory. Increases in activity in the lateral PFC cortex have been typically attributed to the involvement of auxiliary cognitive functions that are crucial during calculation, such as working memory, inhibitory control, and attentional processes (Arsalidou & Taylor, 2011) and these regions are typically more recruited during more demanding problems, such as larger problems, and during the execution of procedural or back-up strategies, when the answer cannot be retrieved from long-term memory. Finally, occipito-temporal regions, including the FG, are involved in the visual processing of symbolic numerical information, given that arithmetic stimuli represent visual symbols (Arsalidou & Taylor, 2011), but the specific role of this region in arithmetic has not been studied in much detail (Peters et al., 2015).

Training studies in adults that have tried to simulate the above-mentioned developmental process of strategy change arithmetic, in particular the development from procedures to arithmetic fact retrieval (Zamarian & Delazer, 2015 for a review). These studies offer a window to our understanding of how arithmetic networks change across skill acquisition. These data revealed, as a function of training, a decrease in PFC coupled with an increase in activity in the posterior parietal cortex. At the same time, activity in the parietal cortex shifts from the IPS to the AG, potentially reflecting the increasing reliance on retrieval strategies and a decreasing reliance on backup strategies, such as counting or decomposition, which is in line the overlapping waves model of strategy development (Siegler, 1996). These data offer insights in how brain activity changes as a function of learning, but these studies in adults are not necessarily directly transferable to children, because children's brains are not merely smaller versions of a highly skilled adult brain (Ansari, 2010). Indeed, adult studies miss important changes in the functional organization of brain networks during schooling (Qin et al., 2014; Rosenberg-Lee et al., 2015) and therefore, studies in developmental populations, as we review below, are crucial to understand the neurophysiological changes that are associated with developmental changes in arithmetic strategy use.

4. Review method

We performed a search of the literature in September 2016 in the Web of Science database with the keywords “arithmetic*”, “children”, and “*MRI”, “DTI”, “EEG”, “NIRS”, or “MEG”. Studies were only included if they reported original empirical data, comprised multiple participants, collected brain imaging measures and if they were reported in an peer reviewed English-language journal. Relevant articles were further added by screening the references and by reviewing citation lists of the articles obtained from the Web of Science search that met our inclusion criteria. This resulted in a final set of studies that summarized in Tables 1-5.

5. Brain activity during arithmetic in children

Most of the existing studies have used fMRI to investigate brain activity in children (Table 1; Figure 1). Only a few studies have used other imaging methods (NIRS: $n = 1$; MEG: $n = 1$; EEG: $n = 6$; ERP: $n = 6$) and their findings will be only very briefly covered in this section.

5.1 Typically developing children

fMRI studies in typically developing children have reported that, as in adults, a widespread, bilateral network of areas shows increases in brain activity during arithmetic (Figure 1; Kaufmann et al., 2016) and such widespread activation has also been observed in ERP (Prieto-Corona et al., 2010; Xuan et al., 2007; Zhou et al., 2011) and EEG (Dimitriadis et al., 2015; Vourkas et al., 2014) studies. Kawashima and colleagues (2004) reported the first developmental fMRI data and compared children and adults during addition, subtraction and multiplication. Children recruited very similar neural networks, including prefrontal, intraparietal and occipito-temporal areas, as adults, and this was largely comparable across the three operations. However, their sample was very small and coupled with a very broad age range of children, this may have made it very difficult to detect developmental differences.

Subsequent studies largely confirmed the involvement of a bilateral fronto-parietal network during calculation. For example, studies examining addition in children have reported increased activation in bilateral frontal and posterior parietal areas (Davis et al., 2009; Kucian et al., 2008; Meintjes et al., 2010; Mondt et al., 2011), but this increase in activity seems to be smaller when directly compared to adults (Davis et al., 2009; Kucian et al., 2008). Similar increases have been observed during subtraction in children (Chang et al., 2016; Mondt et al., 2011; Peters et al., 2016) and adolescents (Chang et al., 2016). These increases in fronto-parietal activity have also been detected with NIRS (Dresler et al., 2009) and MEG (Simos et al., 2008).

These data were a first important step in understanding the brain networks of arithmetic in children, but they did not include systematic task manipulations to unravel how different networks are recruited during various strategies, as is observed in adults (Grabner et al., 2009; Prado et al., 2011; Tschentscher & Hauk, 2014). To address this issue, De Smedt et al. (2011) systematically manipulated problem size (small vs. large) and operation (addition vs. subtraction) in a relatively narrow age range of 10-to-12-year-olds (see Moore et al., (2014) and Van Beek et al., 2014, for a similar manipulation of the problem size effect with ERPs). De Smedt et al. (2011) reasoned that the large vs. small and subtraction vs. addition contrasts would reveal networks that are more important for procedural strategies, whereas the reverse contrasts would unravel networks that are more

relevant to fact retrieval. Their data revealed that, as in adults, subtractions and large problems showed increases in a wide fronto-parietal network that comprised the IPS and PFC (see also Evans et al., 2016). The reverse contrasts, pointing to arithmetic processes that are more related to fact retrieval, however revealed a different pattern than in adults. Instead of the AG, it was the medial temporal lobe, specifically the left hippocampus (HC), that showed increased brain activity during fact retrieval problems. This suggested a specific role of the HC that might be related to the formation of long-term memories of arithmetic facts, a hypothesis that has gained increased attention in the last years (Menon, 2016). These differences between children and adults might be explained by the time-limited role of the hippocampus in long-term memory (Smith & Squire, 2009), with its role being crucial in the early consolidation of (arithmetic) facts, while in later stages of more automatization, posterior parietal systems, including the AG, become more relevant.

The role of the HC in arithmetic fact retrieval has been confirmed in other developmental studies (Menon, 2016, for a review). Cho et al. (2011) studied brain activity during addition in children that were categorized as “counters” or “retrievers” depending on their dominant strategy (i.e. if a child used that strategy on more than 60% of the trials), which was determined via verbal report data prior to scanning. The authors used multivariate pattern analysis (MVPA) techniques (Norman et al., 2006), which allowed them on a much finer scale than univariate fMRI to investigate spatial patterns of activity (in a given region) and compare these patterns between groups. They showed that the counters and retrievers showed distinct patterns of brain activity in the bilateral HC (as well as in medial temporal gyri (MTG), IPS, SMG and AG). This was replicated in children of a similar age range (Cho et al., 2012): Higher frequency of fact retrieval (determined by verbal reports) correlated with increased activity in the bilateral HC (as well as lingual gyri, FG and superior parietal areas). Qin et al. (2014) compared children, adolescents and adults, and further confirmed this time-dependent role of the HC: Children showed increased activity in the bilateral HC, but this activity was significantly lower in adolescents, who in turn, did not differ from adults. MVPA analyses also indicated an increase in inter-problem representational stability in adolescents and adults, compared to children. These data indicate that hippocampal engagement increases in primary school but then decreases and stabilizes in adolescence to reach adult-like levels of activity.

5.2 Developmental changes

The above-mentioned differences between children and adults undoubtedly indicate that these activated brain networks change over developmental time. A handful of studies have aimed to characterize these changes by correlating brain activity with age (Eden et al., 2016; Prado et al., 2014; Rivera et al., 2005), by comparing different age groups (Chang et al., 2015; Davis et al., 2009; Dresler et al., 2009; Kawashima et al., 2004; Kucian et al., 2008; Qin et al., 2014; Rosenberg-Lee et al., 2011), and ultimately, but unfortunately scarcely, by following children longitudinally (Qin et al., 2014).

Rivera et al. (2005) reported the first age-related changes in brain activity during small additions and subtractions in 8- to 19-year-old children. They investigated which areas showed positive (i.e. age-related increase) and negative (i.e. age-related decrease) associations with age, and found age-related increases in activity in the left SMG, and the anterior AG and adjoining IPS, reflecting increased specialization in the left parietal cortex, as well as increases in the lateral occipito-temporal cortex. These data probably reflect the neural changes that are accompanied with an increasing

reliance on fact retrieval and/or increasing automatization of arithmetic facts, as suggested by the overlapping waves model of strategy development (Siegler, 1996). On the other hand, they reported that activity in DLPFC, VLPFC and ACC, decreased with age, potentially reflecting a decrease in reliance on working memory and attentional resources. Interestingly, they also observed a decrease in hippocampal systems with age.

Prado et al. (2014) further investigated whether these age-related changes differed depending on the operation (subtraction vs. multiplication) in 8-to-13-year-old children. Such contrast indirectly reveals something about age-related changes in strategy use, as procedural strategies are more common in subtraction (Barrouillet et al., 2008) while retrieval occurs more frequently in multiplication (Imbo & Vandierendonck, 2008). Prado et al. (2014) used two localizer tasks to investigate brain activity in two clusters of areas, i.e. areas related to numerical magnitude processing in the right posterior parietal cortex (including IPS and posterior superior parietal lobule (PSPL)) with a non-symbolic number comparison task as well as areas related to phonological processing in the left MTG and inferior frontal gyrus (IFG) with a phonological rhyming task. Activity in the areas related to numerical magnitude processing showed an age-related decrease during subtraction, but not multiplication. On the other hand, activity in the left MTG was characterized by age-related increases during multiplication, whereas brain activity during subtraction in this region did not change with age. These data suggest that age-related changes in brain activity during arithmetic are operation dependent: Changes in multiplication correlated with language-related areas, while changes in subtraction correlated with numerical magnitude processing areas. Evans et al. (2016) recently reported operation-dependent age-related changes in an even wider age range (7- to 29-year-olds). They observed age-related increases in right HC and left medial frontal gyrus (MFG) for addition, but not for subtraction – they also found age-related increases in addition and subtraction in the right temporo-parietal cortex and these were similar to age-related changes during a reading task. Evans et al. (2016) interpreted these operation differences as reflecting differences in strategy use, assuming a larger amount of fact retrieval in addition than in subtraction, but no study thus far has directly investigated brain activity during different strategies that children use to solve these problems.

While these studies investigated change across very protracted developmental periods, it remained to be determined whether such changes can be observed over smaller time intervals. Rosenberg-Lee et al. (2011) addressed this by comparing two groups that only differed in one year of schooling. Second and third graders were carefully matched in terms of IQ, reading, working memory and mathematics, and completed an addition task with two complexity levels during fMRI acquisition. They observed that complexity modulated the activity in the PFC differently in the two grades: Second graders showed higher activation differences in the ventromedial PFC, whereas third graders showed larger differences in the left DLPFC. These differences point to a developmental change in the task-appropriate deactivation of the default mode network. The third graders also showed larger activation differences in bilateral IPS and superior parietal lobule, right AG, the right lateral occipital cortex, and the bilateral parahippocampal and lingual gyri. These data suggest that, in addition to the well-established role of the dorsal posterior parietal cortex, also more ventral areas are relevant to calculation, yet their roles have not been studied in detail (Menon, 2015).

Chang and colleagues (2016) recently aimed to further clarify linear as well as non-linear age-related changes in cytoarchitecturally distinct areas in the posterior parietal cortex, by comparing

7-to-10-year-old children, adolescents and adults during subtraction. They observed linear age-related increases in the bilateral ventral anterior IPS (IPS-hIP1) and neighboring SMG (SMG-PFm) and AG (AG-PGa). However, the posterior AG (AG-PGp) did not show age-related changes, indicating that subdivisions of the AG play distinct roles in the development of arithmetic. Non-linear age-related changes were found in the middle SMG (SMG-PF). These age-related changes were interpreted as reflecting changes in strategy use, but such explanation only remains speculative as strategies were not examined in this study. Furthermore, this study, as well as those described above, only involved a cross-sectional comparison of age groups, and age-cohort differences, rather than developmental differences, might explain the observed differences under study. To exclude this confound, a longitudinal follow-up of the same sample of children is needed in order to study how arithmetic networks change over developmental time.

We only found one study that investigated brain activity at multiple time points in one sample of children (Qin et al., 2014). These authors observed within a one-year time frame an increase in activity in the bilateral HC, coupled with a decrease in activity in bilateral DLPFC, left superior parietal lobule and right posterior occipito-parietal areas. These changes were accompanied by behavioral verbal report data that indicated an increased reliance on fact retrieval strategies over one year time. These findings echo the above-mentioned negative correlations between age and brain activity during arithmetic (Rivera et al., 2005), reflecting a decreasing reliance on working memory and executive control that is probably coupled with a decrease of effortful procedural strategies and an increase in arithmetic fact retrieval, as is predicted by the overlapping waves model (Siegler, 1996).

5.3 Individual differences

Imaging data in adults indicate that activity in the arithmetic network is modulated by individual differences (Grabner et al., 2007). Are such differences also observed in children? De Smedt et al. (2011) compared brain activity in children with low and high levels of arithmetic fluency. De Smedt et al. observed that during small problems, children with low arithmetic fluency showed higher activity in the right IPS than those with high fluency. Berteletti et al. (2014) reported a similar pattern of findings and observed a negative association between number line estimation ability and activity in the IPS during subtraction. Similarly, Price et al. (2013) observed in adolescents that low mathematical competence was associated with increased activity in the right IPS during addition and subtraction. More recently, Demir et al. (2014) observed that such patterns are particularly prominent in children with low SES, who are known to have lower levels of mathematical achievement. These data suggest that individuals with lower mathematical competence show higher activity in numerical magnitude processing related areas of the arithmetic network. It could be that poorer representations of magnitude prevent individuals with low mathematical competence to develop advanced mathematical skills. Alternatively, this increased IPS-activity might reflect a protracted reliance on immature arithmetic procedures, such as counting, that require more numerical magnitude processing. Future studies should further investigate these possibilities.

Price et al. (2013) also showed that adolescents with higher mathematical competence showed higher levels of activity in the left SMG and ACC, as had been observed in adults (Grabner et al., 2007), but such associations have not been found in (younger) children. As reviewed above, HC rather than temporo-parietal regions are more crucial for fact retrieval earlier in development.

Interestingly, Cho et al. (2012) reported individual differences in HC activity, showing that children with high retrieval fluency had higher HC-activity.

5.4 Atypical development

Persistent deficits in arithmetic are the key feature of dyscalculia (e.g., Geary, 1993, 2011) but only a minority of studies examined the neural underpinnings of this neurodevelopmental disorder. Most of available studies focused on numerical magnitude processing as an underlying correlate of the observed mathematical deficits (De Smedt et al., 2013; Kucian & von Aster, 2015, for reviews) but surprisingly few have investigated brain activity during arithmetic in this population (Table 1).

Some studies (Davis et al., 2009; Rosenberg-Lee et al., 2015; Simos et al., 2008) reported increased activity in a wide-spread network of regions, including parietal, prefrontal and occipito-temporal regions, in dyscalculia during addition and subtraction, and these differences do not merely reflect performance differences (Rosenberg-Lee et al., 2015). These authors also observed that the increases in brain activity were particularly prominent in subtraction, which is more difficult than addition and which relies to a larger extent on procedural strategies, in posterior parietal areas (including bilateral IPS, SPL and AG) and the left FG.

On the other hand, decreased brain activation in children with dyscalculia, coupled with the observation that no brain areas showed increased activity in dyscalculia compared to age-matched controls has also been reported. Ashkenazi et al. (2012) compared the brain responses during simple (i.e., + 1) and more complex (single-digit) additions. They found decreased activity in dyscalculia in a wide-spread network of regions, including bilateral PFC, right posterior parietal and occipito-temporal areas. This was further explained by the lack of difficulty-related modulation of neural activity in these regions in dyscalculia: Typically developing children showed increased activity for complex compared to simple problems in these areas, whereas children with dyscalculia did not, a pattern that also has been observed in children with low arithmetical fluency (De Smedt et al., 2011). Multivariate representational similarities further revealed that, in the bilateral IPS, the patterns of brain activity during simple and complex problems were less distinguishable in children with dyscalculia (Ashkenazi et al., 2012), again reflecting a lack of difficulty-related modulation in the neural activation patterns of children with dyscalculia. Berteletti et al. (2014) focused on multiplication and used a localizer approach in which areas related to number processing (i.e., right PSPL and IPS) and to language processing (left IFG and left MTG) were delineated with a non-symbolic number comparison task and rhyming task, respectively. Children with dyscalculia showed reduced activity in these ROIs, leading the authors to conclude that numerical as well as language-related processes in multiplication are impaired in dyscalculia.

Impairments in arithmetic, in particular fact retrieval, have also been described in children with dyslexia (e.g., De Smedt & Boets, 2010; Simmons & Singleton, 2008), a specific neurodevelopmental learning disorder of which persistent deficits in learning to read is the hallmark feature (e.g., Snowling, 2000). The brain networks that support reading and arithmetic are overlapping in the temporo-parietal and inferior frontal cortices (De Smedt et al., 2010; Prado et al., 2011) and individual differences in arithmetic fact retrieval correlate with white matter integrity of the arcuate fasciculus (AF) (Van Beek et al., 2014), a tract that traditionally has been related to individual differences in language and reading ability, and is impaired in dyslexia (Vandermosten et al., 2012). At the behavioral level, the high correlation between reading and arithmetic fact retrieval is well

documented and may reflect the forming of associative relations, for example, between letters and sounds or between arithmetic problems and their answers (e.g., Chu et al., 2016; Fuchs et al., 2016; Koponen et al., 2013). In view of this overlap between reading and arithmetic, one fMRI study has contrasted the brain responses during addition and subtraction in children with and without dyslexia (Evans et al., 2014). These authors observed decreased activation in the left SMG in dyslexia, in line with the decreased activity in language-related areas in these children (Eden et al., 2016). Evans et al. (2014) also observed a group by operation interaction in the right inferior parietal lobe, which echoes the above-mentioned data in children with low arithmetical fluency (De Smedt et al., 2011): Typically developing children recruited this area more during subtraction than addition, while children with dyslexia did not show such modulation.

Findings from children with atypical arithmetical development remain mixed today as both increases and decreases in activity in the arithmetic network have been reported. There are currently too few studies available to draw definitive conclusions and this is further complicated by study differences in criteria used to include participants as well as wide age-ranges, which might mask important developmental changes in children with atypical development. Future studies in narrow age bands are therefore crucial to make headway. It would also be interesting to investigate the differences in brain activity between children with dyscalculia and dyslexia. Both conditions show impairments in arithmetic, but their neural origin might be different. Recent data by Peters et al. (submitted) contrasted brain activity during arithmetic in typically developing children, children with dyscalculia, children with dyslexia and children with both dyslexia and dyscalculia. Surprisingly, the brain activity profiles of these three groups of learning disorders showed high similarity and this suggests that these neural profiles may be more overlapping than originally thought.

Is it possible to change brain activity during arithmetic in atypical populations via targeted interventions? Only two studies investigated this question (Iuculano et al., 2015; Kesler et al., 2011), and this clearly represents an important agenda for future studies. Kesler et al. (2011) ran a pilot study in 7-to-14-year-old children on the effect of a numerical magnitude processing training on brain activity during two-digit calculation. They observed increases in bilateral superior parietal cortex and decreases in frontal, temporal and HC areas following training, indicating that activity in these areas is malleable. The findings are however hard to interpret in the absence of a control group. Recently, Iuculano et al. (2015) offered eight weeks of one-on-one math tutoring intervention, which focused on efficient counting strategies and learning arithmetic facts in children with dyscalculia and age-matched controls. Before training, children with dyscalculia showed increased activation during single-digit addition in frontal, superior parietal, temporo-parietal, and hippocampal areas. After training, their brain activity did not differ from age-matched controls anymore. MVPA further showed that a classifier could reliably discriminate brain activity patterns of children with dyscalculia and age-matched controls before, but not after training, suggesting normalization of brain activity in dyscalculia after intervention.

6. Connectivity between areas of the arithmetic network

The above-reviewed functional imaging data clearly indicate the involvement of multiple distant brain regions in arithmetic. This highlights that in order to fully understand the neural basis of arithmetic and its disorders, one needs to study the connectivity between these regions rather than merely focusing on isolated brain areas (Uddin et al., 2010, for a discussion). We summarize studies

that have investigated task-based functional connectivity (Table 2), studies that have correlated resting-state connectivity networks to arithmetic performance (Table 3) and studies of structural connectivity that used diffusion tensor imaging (DTI) to investigate associations between white matter tracts and arithmetic (Table 4; Figure 1).

6.1 Task-based functional connectivity

Six of the above-mentioned fMRI studies also investigated task-based functional connectivity. This work has revealed the importance of fronto-parietal (Chang et al., 2016; Rosenberg-Lee et al., 2015, 2011), hippocampal-frontal (Cho et al., 2012; Qin et al., 2014) and hippocampal-parietal (Qin et al., 2014) connectivity.

Rosenberg-Lee et al. (2011) reported increases in the functional connectivity during addition between left DLPFC and posterior parietal areas from second to third grade. Chang et al. (2016) further suggested that this change might be non-linear as they observed increased functional connectivity during addition in adolescents compared to children and adults, who did not differ in their connectivity profiles. Increased parietal-frontal functional connectivity has also been observed in 7-to-9-year-old children with dyscalculia compared to age-matched controls (Rosenberg-Lee et al., 2015). These parietal-frontal circuits have been linked to working memory systems that are recruited during arithmetic (see Menon, 2016, for a review). However, these connectivity differences between ages and ability groups are not so easy to interpret, because increased connectivity might reflect increasingly efficient use of working memory resources or compensatory effects in individuals with lower ability (Menon, 2016). Also, the number of task-based functional connectivity studies is currently too few to draw definitive conclusions. Future research, preferably with longitudinal designs, is needed to further examine this.

Cho et al. (2012) and Qin et al. (2014) reported increases in hippocampal-PFC connectivity during addition with increasing age and retrieval ability. Cho et al. (2012) demonstrated that higher addition-related connectivity between the right HC and PFC was associated with higher fact retrieval fluency. In their longitudinal data, Qin et al. (2014) observed that increases in hippocampal connectivity with PFC and parietal areas during addition were associated with individual gains in arithmetic fact retrieval. Qin et al. (2014) also demonstrated that changes in hippocampal connectivity rather than regional changes in the HC itself, predicted children's increase of arithmetic facts. This confirms that increases in arithmetic fact retrieval are related to functional connectivity in hippocampal-neocortical circuits, further supporting the role of declarative memory systems in fact retrieval. These interactions between the HC and neocortex are probably not exclusively relevant to learning arithmetic, but play a broader role in memory formation and knowledge acquisition (e.g., McClelland et al., 1995).

6.2 Resting-state connectivity

Individual differences in arithmetic have also been correlated with connectivity between brain regions during rest (*rsfMRI*). Evans et al. (2015) found that increased intrinsic connectivity between different areas of the arithmetic network, including DLPFC, posterior parietal regions, ventral occipito-temporal regions and anterior temporal regions at the age of 8, predicted subsequent growth in arithmetic. In their intervention study that investigated the effect of an 8-week one-on-one tutoring focusing on efficient counting and improving retrieval fluency, Supekar et al. (2013) showed

that intervention gains in addition were predicted by resting-state hippocampal-PFC connectivity, with individuals with higher intrinsic connectivity showing larger intervention gains. Combining data from various earlier studies (Ashkenazi et al., 2012; Luculano et al., 2015; Rosenberg-Lee et al., 2015; Supekar et al., 2013), Jolles et al. (2016) investigated the intrinsic connectivity of the IPS in age-matched typically developing children and children with dyscalculia. The IPS showed strong intrinsic connectivity with multiple areas of the arithmetic network, including bilateral PFC, parietal and ventral occipito-temporal regions. Group comparisons further revealed that children with dyscalculia showed increased interhemispheric IPS connectivity and increased connectivity between the IPS and (dorsal) fronto-parietal regions. Additional analyses showed spontaneous increases in low frequency fluctuations during rest in IPS and other regions in children with dyscalculia. Pattern classification algorithms were able to reliably discriminate children with and without dyscalculia on the basis of their connectivity data, leading the authors to suggest that IPS-connectivity might represent a biomarker for dyscalculia. However, in order to be a reliable biomarker, it remains to be seen whether such hyper-connectivity profiles are specific to dyscalculia or can also be observed in other neurodevelopmental conditions.

Jolles, Supekar, et al. (2016) recently investigated changes in IPS intrinsic connectivity following the above-mentioned math tutoring intervention (Supekar et al., 2013). Jolles, Supekar et al. (2016) observed increases in IPS intrinsic connectivity with PFC, ventral occipito-temporal cortex as well as HC. Increases in IPS connectivity were positively correlated with performance gains in the intervention. These studies are only but a first step to investigate how intrinsic connectivity is related to arithmetic. Future studies are needed in order to carefully specify these individual differences in intrinsic connectivity and how they change as a function of development, ability level and interventions. At least, the available data highlight the need for a multisystem approach rather than an isolated study of specific brain regions.

6.3 Structural connectivity

Structural connections between regions of the arithmetic network can be investigated by means of DTI, which allows one to correlate behavioral performance with the integrity of white matter tracts as indexed by fractional anisotropy or FA (Matejko & Ansari, 2015; Vandermosten et al., 2012 for excellent reviews on DTI studies in arithmetic and reading, respectively). Studies in typically developing children have revealed significant associations between left temporo-parietal white matter, i.e. the superior corona radiata (CR), and calculation in children (van Eimeren et al., 2008) and adolescents (Matejko et al., 2013). Significant positive associations between arithmetic and the superior longitudinal fasciculus (SLF), which connects the posterior parietal cortex with the PFC have also been observed (Li et al., 2013; Matejko et al., 2013; Tsang et al., 2009). Similar associations were reported for the inferior longitudinal fasciculus (ILF; Li et al. 2013; van Eimeren et al., 2008), which connects PFC with ventral occipito-temporal areas.

Investigating how different operations were related to white matter connections between the frontal and temporo-parietal cortex, Van Beek et al. (2014) focused on the AF, a tract that has been often investigated in reading research (e.g., Vandermosten et al., 2015). Van Beek et al. (2014) found that the integrity of the left anterior part of the AF, connecting the frontal and parietal cortex, was positively correlated with addition and multiplication, but not with subtraction and division, suggesting a role for the AF in fact retrieval. Follow-up analyses revealed that this was explained by a

close relationship between reading and fact retrieval, as the association between the AF and fact retrieval disappeared when controlling for pseudoword reading. This was interpreted as reflecting a common reliance on phonological codes in (pseudoword) reading and arithmetic (e.g., De Smedt, 2016; Simmons & Singleton, 2008).

Jolles, Wassermann, et al. (2016) recently examined whether different sections of the SLF, which connects frontal to parietal to temporal regions, were related to training-induced changes in arithmetic. The study design was similar to Supekar et al. (2013), and Jolles, Wassermann, et al. (2016) showed that specifically the part of the SLF that connects the frontal and temporal regions, predicted the learning gains in addition and subtraction.

Studies on atypical mathematical development, including children with dyscalculia (Ranpura et al., 2013; Rykhlevskaia et al., 2009), velocardiofacial syndrome (Barnea-Goraly et al., 2005), multiple sclerosis (Till et al., 2011), fetal alcohol syndrome (Lebel et al., 2010) and premature children (Pavlova et al., 2009) have also reported reduced white matter integrity, particularly in the SLF and in temporo-parietal white matter, compared to age-matched controls. These studies further confirm the role of the white matter tracts that connect distinct parts of the arithmetic network.

It is important to emphasize that all the existing DTI studies are cross-sectional and no longitudinal data are available. Such data are really needed to find out how the quality of white matter tracts of the arithmetic network develops as children become more proficient. Furthermore, most of the above-mentioned studies involved samples of children with very wide age ranges (e.g., 7-11 or 10-15 years) but these long developmental periods are characterized by massive changes in white matter (Giedd & Rapoport, 2010) as well as arithmetic, which might confound the observed correlations between white matter and arithmetic. This requires future studies to include children of more narrow age ranges. Finally, white matter in the parietal cortex (but also as in other places throughout the cortex) is characterized by multiple crossing fibers, because many tracts intersect in this cortical area (Figure 1). For example, white matter in the above-mentioned temporo-parietal areas that correlates with arithmetic, includes intra-hemispheric (AF), inter-hemispheric (posterior part of the corpus callosum) and cortico-spinal (CR) connections. The analysis of DTI data via the classic tensor model, as was done in all reviewed studies, is problematic because it does not allow one to estimate these crossing fibers and as such provides an oversimplification of the underlying anatomy (Dell'Acqua et al., 2012), leaving it unresolved which of these tracts is relevant for individual differences in arithmetic. This can be resolved with non-tensor models, such as spherical deconvolution, which provide a more fine-grained analysis of white matter tracts and their crossing fibers in the brain (Farquharson et al., 2013). To our knowledge, there are no studies that used spherical deconvolution in the studies about arithmetic.

7. Structure of the arithmetic brain network

Voxel-based morphometry studies have investigated how anatomical characteristics (in particular grey matter) of the above-mentioned regions arithmetic brain network are correlated with performance. The first structural imaging studies compared children with difficulties in arithmetic to age-matched controls and showed reduced grey matter in distinct areas of the above-mentioned arithmetic network (Han et al., 2013; Isaacs et al., 2001; Ranpura et al., 2013; Rotzer et al., 2008; Rykhlevskaia et al., 2009). The first structural data were reported by Isaacs et al. (2001) and revealed that adolescents with very low birth weight and calculation deficits had smaller grey matter volume

in the (left) IPS. Subsequent studies in children with dyscalculia showed that they had reduced grey matter in the posterior parietal cortex (including IPS) (Ranpura et al., 2013; Rotzer et al., 2008; Ryklevskaia et al. 2009), in frontal areas, such as IFG and MFG, (Rotzer et al., 2008), in the parahippocampal gyrus (Ranpura et al., 2013; Ryklevskaia et al. 2009) and in the occipito-temporal cortex (Han et al., 2013; Ryklevskaia et al. 2009).

Surprisingly few studies have examined this association between grey matter and arithmetic in typically developing children. Significant positive associations were observed between grey matter volume in the left IPS and arithmetic in 6-7-year-olds (Price et al., 2016) and 9-10-year-olds (Li et al., 2013). Supekar et al. (2013) further showed that the volume of the right HC predicted the learning gains of a one-on-one tutoring intervention that focused on efficient counting and fact retrieval, with larger hippocampal volumes before the intervention predicting larger intervention gains, again confirming the role of the HC in arithmetic fact retrieval. Finally, Evans et al. (2015) reported that grey matter volumes of various parts of the arithmetic network, i.e., posterior parietal areas, and ventral occipito-temporal cortex, predicted the growth in arithmetic across primary school. All these data confirm that the structural integrity of different parts of the arithmetic network is positively correlated with arithmetic performance. On the other hand, studies are needed to investigate how these structural properties of the network and their change as a function of time, ability level and interventions, are related to the brain activity that is occurring when children perform arithmetic.

8. Challenges and future directions

The existing body of brain imaging studies on arithmetic has clearly increased over the last five years. There are emerging trends in our understanding of the functional and structural properties of the arithmetic network in children, but the literature remains scattered to date, particularly in the context of atypical development. Meta-analyses of brain imaging data (see Turkeltaub et al. (2002), for a discussion in the field of reading) are therefore key in order to synthesize the existing studies with inconsistent findings, but this will require a more critical mass of studies than what is currently available. For example, Eickhoff et al. (2016) recommended to include at minimum 17-20 experiments to have enough power to detect a moderate effect. This number obviously increases if one aims to include a test of moderators of the arithmetic network, such as age, ability level or arithmetic task. Such numbers of brain imaging studies are currently not available in the field of arithmetic development.

8.1 Truly understanding development

Many of the above-reviewed studies, whose aim was specifically to investigate age-effects, included samples of very wide age ranges. This is problematic for studying arithmetic, because schooling or instruction, even over a short duration of one year results in changes in brain activity (Rosenberg-Lee et al., 2011), and we can only but speculate on its effects on connectivity and brain structure. If we truly want to understand development, studies should orient their focus to relatively narrow windows of schooling in order to understand how gradual changes occur over time (Karmiloff-Smith, 2010) – note that this window of schooling does not necessarily correspond to a specific chronological age. This should be done in windows during which development is the steepest, or stated differently, instructional attention to a given skill is the largest. In arithmetic, this should be from first to third grade, during which the largest changes in strategies are occurring. The comparison of focused groups, who are comparable in their instructional level, clearly presents a first

step in this endeavor, yet longitudinal data are critical to make headway. These questions about development can also be addressed by focused short-term training studies, as has been done in adults (Zamarian & Delazer, 2015), which experimentally manipulate the transition from procedure-based arithmetic to fact retrieval.

8.2 Atypical development

The absence of longitudinal data is particularly problematic in atypical development. The existing data do not allow us to determine whether the functional and structural abnormalities seen in these atypical conditions are the cause or the consequence of their difficulties in arithmetic. It could be that the reported abnormalities are simply due to differences in arithmetic experience and that they do not represent the etiology of a specific learning disorder. For example, reading studies on dyslexia, that compared children with dyslexia to age-matched controls and to children who had a similar reading level and experience but were younger in age (reading-level matched), revealed that some of the observed functional (e.g., Hoeft et al., 2007) and structural (e.g., Krafnick et al., 2014), neurobiological abnormalities in dyslexia are explained by their reduced reading experience and do not represent the etiology of dyslexia (Norton et al., 2015, for a review). Such comparisons with ability-level matched children are non-existent in brain imaging studies on dyscalculia and clearly represent an area for future research.

We also do not know whether these abnormalities in atypical conditions, particularly those related to structure and connectivity, are already present before children learn to calculate, and hence may represent a neurobiological cause of their disability. The availability of child-friendly brain imaging protocols makes it possible to study the brain in children before they learn to calculate. In dyslexia research, there is now an increasing number of brain imaging studies that have investigated pre-readers, including at-risk children (see Vandermosten et al., 2016, for a meta-analysis). Similar studies in the arithmetic domain are crucial in order to further establish the neurobiological cause of atypical arithmetic development. The longitudinal follow-up of these young children is also needed to understand how brain circuits develop when they learn to calculate and how these change when children acquire different arithmetic strategies. Beyond adding to our understanding of atypical development, these studies will inform us about how educational experiences change brain structure and function, further revealing insights on experience-dependent plasticity in children.

8.3 Measures of arithmetic

The measurement of arithmetic skill in future brain imaging studies clearly requires careful attention. The above-reviewed fMRI-studies vary greatly in the arithmetic tasks and baseline conditions they used and in their dependent variables when studying brain-behavior correlations. This makes the current evidence difficult to interpret, because different aspects of the arithmetic task will modulate the arithmetic network. Inconsistencies between studies, particularly in the context of atypical development, might be explained by the selection of an appropriate baseline condition and by how this baseline conditions affects activation levels in the parietal cortex (Menon, 2016, for a discussion).

This review started by highlighting that a crucial characteristic in children's arithmetic development involves a change in the mix of strategies they use (Geary, 2011; Jordan et al., 2003; Siegler, 1996). None of the reviewed brain imaging studies, however, has provided a direct measure

of these strategies. Instead, they all relied on indirect measures, such as contrasting different operations or problem sizes, an approach that has been severely criticized (De Smedt, 2016), already for a long time (Siegler, 1987). This is even more problematic in developmental research and atypical development, where there are massive changes in children's strategic development and problems of a given type (i.e. size or operation) will be solved by different strategies depending on the age, education or ability level. The existing brain imaging data have interpreted differences between operations or problem sizes as reflecting differences in strategies, but they never provided direct measures of these strategies to bolster these conclusions. Studies in adults have shown that it is possible to analyze brain activity on an item level as a function of verbally reported strategies (Grabner et al., 2009; Grabner & De Smedt, 2011; Tschentscher & Hauk, 2014), showing that it is the strategy and not the operation that modulates the arithmetic network. Interestingly, similar data became recently available in children (Polspoel et al., submitted), pointing to very similar conclusions.

8.4 Environmental effects

Arithmetic represents a culturally transmitted skill that is obviously not acquired in isolation. Nearly all of studies discussed in this review included children from Western countries (US and Western Europe), the majority of whom were English-speaking, and this needs to be taken into account when evaluating the findings from studies that are currently available. There is massive impact of the home and educational environment on children's arithmetic development (e.g., Geary, 1996) and consequently on the development of its underlying brain networks. These contextual cross-cultural differences have been ignored in brain imaging studies. For example, there are large differences between Western countries in which arithmetic strategies are instructed, ranging from a continuing emphasis on counting in some countries vs. an early discouraging of counting (even prohibition) in order to promote fact retrieval (De Smedt, 2016, for a discussion). Such instructional differences, combined with the emphasis a curriculum places on arithmetic fact retrieval – the so-called math wars (Schoenfeld et al., 2006) – inevitably will affect the emergence and organization of the arithmetic brain network. In fact, there are adult training data who demonstrate that activity in the arithmetic network is modulated depending on the type of instruction, i.e., learning by strategies or by drill (Delazer et al., 2005). It is also important to emphasize that one year of instruction in a particular culture (e.g., US or Western Europe) does not necessarily result in the same level of expertise as one year of instruction in other cultures (e.g. East Asia). Similarly, instruction that occurs during the maturation of critical white matter tracts, may not be the same as instruction that occurs earlier or later. It would therefore be interesting to run studies to investigate the divergences and communalities between children who are enrolled in different math curricula that differ in their emphasis on arithmetic fact retrieval at different stages of learning arithmetic. At the very least, future brain imaging studies on arithmetic should carefully document the educational context in which the data have been collected as this is crucial to understanding the data. This contextual description makes studies in educational neuroscience also more educationally relevant and allows for more potential bridges between cognitive neuroscience and classroom learning (De Smedt & Grabner, 2015).

8.5 It's not just the parietal cortex

The present review clearly indicates that arithmetic development and its disorders are not confined to one particular brain area, but rather suggests the involvement of a broad and dynamic network, that changes over time. The interactions between these different components need to be better understood. One example deals with the understanding of the role of the ventral occipito-temporal cortex in calculation. As reviewed above, this area is reliably activated during calculation and structural connectivity in these ventral visual areas is related to individual differences in calculation. The importance of higher-order visual processing in calculation has been highlighted for a long time (Menon et al., 2000), but its role, presumably related to symbolic number representations, has received little attention so far (Menon, 2015). Future studies should therefore determine how these ventral visual circuits interact with other components of the arithmetic network during different arithmetic strategies and how this changes as a function of development and ability level. The controlled manipulation of number representations during the acquisition of brain imaging data and their interaction with arithmetic might allow us to understand the functional role of these ventral areas in calculation and its development (see Peters et al., 2015).

8.6 Methodological advances

The existence of distant but connected nodes of the arithmetic network also requires data-analytic techniques to account for this interconnectivity and as a result, the mere univariate approach that investigates brain activity in (a set of) particular brain regions may not fully capture this complexity. Multivariate approaches, such as MVPA (e.g., Norman et al., 2006) or representational similarity analyses (Kriegeskorte et al., 2008), allow us to study of patterns of brain activity, providing a much more fine-grained understanding of neural representations in a given area or network of areas (Raizada et al., 2010). It might be that there are more subtle differences between different types of strategies in different areas of the brain, for example in IPS, that go undetected if one only uses univariate approaches. These multivariate approaches have been successfully applied in children (Cho et al., 2011), but clearly represent an avenue for future studies. These techniques allow us to investigate how representations change over developmental time (e.g., early stages of fact retrieval vs. fully automated stages; see Qin et al., 2014). They also might capture individual differences between learners, for example by showing less precise representations in one versus the other group.

The vast majority of the reviewed studies have used MRI-techniques and the use of other brain imaging methods to study the arithmetic brain is extremely limited. MRI-data are limited in capturing the temporal dynamics of the calculation process. There is a need for future studies to investigate this precise time course of brain activity during calculation, for example by using EEG/ERP or MEG. Such data could be particularly informative to understand if and when numerical representations are activated during calculation. The combination of these data with those obtained from standard MRI-studies will provide a more fine-grained picture of the arithmetic network and its dynamics.

8.7 Connections between arithmetic and reading

In this review, we have often drawn parallels between the (atypical) development of arithmetic and reading, and their underlying neurocognitive correlates. Until now, these strands of research have been executed in relative isolation of each other, even though both involve the acquisition of

symbolic representations (letters vs. numbers), they both show similar developmental changes in strategy use (from time-consuming processing to direct retrieval of information from long-term memory), their disorders often co-occur and parts of their neural networks are overlapping (e.g., Geary, 1993; De Smedt et al., 2010, for a discussion). It is therefore imperative that future studies jointly study both reading and arithmetic in one sample of children to find out similarities and differences in the neural networks of both academic abilities, and such studies are starting to emerge (Evans et al., 2016). These studies will help us to more fully understand how our brains are able to acquire complex culturally transmitted symbolic skills. They will also help us to understand how much of the differences between typically and atypically developing children can be attributed to domain-general differences and how much of these can be explained by domain-specific factors.

9. Conclusion

Arithmetic is a crucial stepping stone in children's mathematical development and is fundamental in our western everyday life. The study of the brain networks that support this culturally transmitted skill in children is fairly recent, and the existing body of brain imaging studies is only but starting to reveal the functional and structural properties of the arithmetic network in children. This network involves a large set of interconnected areas that include bilateral frontal (DLPFC, VLPFC), parietal (IPS, AG, SMG), occipito-temporal and medial temporal, including HC, areas. This network undergoes developmental changes in its function, connectivity and structure, which are not yet fully understood. There are some parallels of this network with what has been observed in adults, but it is clear that children recruit different networks, particularly during the development of arithmetic facts. Despite these emerging trends, the developmental imaging literature remains scattered and this is particularly the case in the context of atypical development, where there are currently too few studies to make a definitive conclusion. Future studies should therefore include more carefully selected samples of typically and atypically developing children in narrow age bands. The observation that arithmetic involves a wide-spread distributed network of areas highlights the need for connectivity analyses and complex analytic approaches that investigate patterns of brain activity. These methodological advances, coupled with a careful design of the arithmetic tasks and assessments of strategies under study, are likely to produce a more comprehensive understanding of how the arithmetic brain unfolds in children, how it changes over time, and how it is impaired in atypical development.

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Table 1**Summary of studies on brain activity during arithmetic in children**

	Study	Method	<i>N</i>	<i>M</i> _{age}	Age range	Sample	Analysis	Task	Conditions	Additional covariates	Main findings
1.	Kawashima et al. (2004)	fMRI	8	11.6	9-14	TD	Uni	+, -, x			Children ≈ adults
			8	44.1	40-49		WB				PFC, IPS and OT
2.	Rivera et al. (2005)	fMRI	17	13.7	8-19	TD	Uni	+, -		Age	SMG, IPS ↑ with age
							WB				PFC, HC ↓ with age
3.	Rocha et al. (2005)	EEG	20	7.6	?	TD	Uni	Arithmetic			Distinct patterns of neuronal recruitment for different operations
			24	8.4	?						
			20	28	?						
4.	Xuan et al. (2007)	ERP	38	9	8-9	TD	Uni	Arithmetic			Age-related differences in frontal negativity and parietal ERPs
			26	23	22-25						
5.	Kucian et al. (2008)	fMRI	10	9.2	?	TD	Uni	+	Exact		Lowered IFG and IPS activity in children
			10	12.0			WB		Approximate		
			20	27.2							
6.	Simos et al. (2008)	MEG	25	10.4	8-14	TD	Uni	+			DC had ↑ parietal and PFC than DLDC and TD
			14	9.7	8-11	DC	WB				
			16	10.2	8-12	DLDC					
7.	Davis et al. (2009a)	fMRI	27	8.1	7-9	TD	Uni	+	Exact		↑ fronto-parietal areas
			10	30.7	25-49		WB		Approximate		Adults > children
8.	Davis et al. (2009b)	fMRI	24	8.2	8-9	TD	Uni	+	Exact		Frontal and parietal hyper-activation in DC
			24			DC	WB		Approximate		
9.	Dresler et al. (2009)	NIRS	46	10.0	9-10	TD	Uni	+	Digits		↑ fronto-parietal areas
			44	13.9	13-14		WB		Word problems		No age- or format effects
10.	Meintjes et al. (2010)	fMRI	14	10.5	8-12	TD	Uni	+			↑ fronto-parietal areas
							WB				

11.	Prieto-Corona et al. (2010)	ERP	16 18	10.3 26.11	9-12 ?	TD	Uni	x			Differences in N400 and LPC in adults vs. children during retrieval
12.	Cho et al. (2011)	fMRI	19 17	8.2 8.6	7-9 7-9	Retrievers Counters	Uni WB Multi	+			Retrievers had ↑ L-VLPFC, Distinct neural patterns for retrievers vs. counters in HC, L-VLPFC and PPC
13.	De Smedt et al. (2011)	fMRI	8 10	11.9 11.7	10-12 10-12	LAF TAF	Uni WB	+, -	Small Large		Large: ↑ fronto-parietal Small: ↑ L-HC LAF had ↑ R-IPS for small
14.	Kesler et al. (2011)	fMRI	15	10.9	7-14	Turner Syndrome	Uni WB	+, -, x	Single-digit Two-digit	Number sense training	Training effects: ↑ superior parietal ↓ in PFC and HC
15.	Mondt et al. (2011)	fMRI	24	9.6	7-11	Bilinguals	Uni WB	+, -		Language instruction	Instruction in school-language: ↑ left-lateralized and more focal activation
16.	Rosenberg-Lee et al. (2011)	fMRI	45 45	7.7 8.7	7-8 7-9	TD	Uni WB	+	Simple (+ 1) Complex		↑ with grade: Parietal, DLPFC ↓ with grade: Ventre-medial PFC
17.	Zhou et al. (2012)	ERP	22 22	7.8 21.5	7-8 18-26	TD	Uni	+, x			Both groups showed frontal and parietal N400 Adults vs. children: ↑ left frontal N400 Children vs. adults: ↑ right parietal N400
18.	Ashkenazi et al. (2012)	fMRI	17 17	8.12 8.17	7-9 7-9	TD DC	Uni WB Multi	+	Simple (+ 1) Complex		Hypo-activation in DC in PFC, right PPC and OT

											Activation patterns between complex and simple less differentiated in DC in IPS
19.	Cho et al. (2012)	fMRI	86	8.2	7-9	TD	Uni WB	+		Retrieval fluency	↑ retrieval fluency correlates ↑ HC, lingual gyri, FG, superior parietal
20.	Price et al. (2013)	fMRI	33	17.9	17-18	TD	Uni WB	+, -		Math competence (PSAT)	R-IPS is negatively correlated with PSAT L-SMG is positively correlated with PSAT
21.	Berteletti et al. (2014)	fMRI	20	11.6 11.5	8-13 8-13	TD DC	Uni ROI	x			Hypo-activation in DC in left IFG, MTG and right PSPL and IPS
22.	Evans et al. (2014)	fMRI	20	10.2 10.4	9-11 9-11	TD DL	Uni WB	+, -			↓ L-SMG in DL Atypical right inferior parietal modulation in DL
23.	Moore et al. (2014)	ERP	20	9.9 10.1	9-10 9-10	High fit Low fit	Uni	+	Small Large		Effects of problem size on P1, N170, P3, N400 Fitness modulates ERPs
24.	Prado et al. (2014)	fMRI	34	11.1	8-13	TD	Uni ROI	-, x	Small Large		Age-related increases: L MTG in multiplication R PSPL in subtraction Age-related decreases: L IFG in multiplication
25.	Qin et al. (2014)	fMRI	28 20 20	8.3 15.61 20.50	7-9 14-17 19-20	TD	Uni WB	+		Two time points in children	Children had higher HC than adolescents and adults Longitudinal data: ↑ in HC ↓ in DLPFC, SPL and OT
26.	Van Beek et al. (2014)	ERP	22	11.9	11-12	TD	Uni	+	Small Large		Problem size effect on N2 and LPC

27.	Vourkas et al. (2014)	EEG	20 31	9.9 9.7	8-9 8-9	LAF HAF	Uni	+, -		Task difficulty effect in EEG patterns Theta band shows more distributed processing Alpha band had greater network integration
28.	Berteletti et al. (2015)	fMRI	39	11.3	8-13	TD	Uni WB	-	Number line estimation	Negative association between IPS activity and number line estimation
29.	Chang et al. (2015)	fMRI	28 28	8.9 20.4	7-10 19-22	TD	Uni WB Multi	+, -		Adults had larger representational similarity between problems in IPS, PSPL, DLPFC and ventral OT
30.	Dimitriadis et al. (2015)	EEG	20 25	? ?	8-12 21-26	TD	Uni	Arithmetic comparison		Increased functional segregation of network organization younger children
31.	Iuculano et al. (2015)	fMRI	15 15	8.5 8.7	7-9 7-9	TD DC	Uni WB Multi	+	Math tutoring	Pre-tutoring: Hyper-activation in DC in PFC, parietal and HC Classifier discriminates TD and DC Post-tutoring: DC = TD Classifier does not discriminate
32.	Rosenberg-Lee et al. (2015)	fMRI	20 16	8.44 8.34	7-9 7-9	TD DC	Uni WB	+, -	Simple (+ 1) Complex	Hyper-activation in DC in PFC, parietal and OT
33.	Van Beek et al. (2015)	ERP	16 16	10.7 10.8	7-12 7-12	TD mTBI	Uni	+	Small Large	Smaller LPC in mTBI

34.	Chang et al. (2016)	fMRI	25 19 26	8.8 15.7 20.6	7-10 13-17 19-22	TD	Uni ROI	-			IPS activity increases with age Posterior AG shows no age effects
35.	Demir-Lira et al. (2016)	fMRI	33	10.9	8-13	TD	Uni ROI	-		SES	SES moderates effect of math fluency on R-IPS and L-MTG activity
36.	Evans et al. (2016)	fMRI	30	?	7-29	TD	Uni WB	+, -		Age	Age-related increases in R-HC and L-MFG for + but not – Age-related increases in R-temporo-parietal
37.	Kim et al. (2016)	EEG	44 53	? ?	6-17 6-17	TD ADHD	Uni	-			Theta-phase-gamma-amplitude coupling was reduced in ADHD vs. TD
38.	Peters et al. (2016)	fMRI	22	10.7	9-12	TD	Uni WB	-	Subtraction with dots, digits and number words		Dots ↑ Fronto-parietal Digits/Number words ↑ AG, SMG

Note. ADHD = attention deficit hyperactivity disorder. DC = dyscalculia. DL = dyslexia. DLDC = comorbid dyslexia/dyscalculia. LAF = low arithmetical fluency. L = Left. LPC = late positive component. mTBI = mild traumatic brain injury. Multi = Multivariate fMRI analysis. OT = occipito-temporal areas. PPC = Posterior Parietal Cortex. PSAT = Preliminary Scholastic Aptitude test. R = Right. ROI = region of interest approach. TAF = typical arithmetic fluency. TD = Typically developing children. Uni = Univariate fMRI analysis. WB = whole brain analysis.

Table 2**Summary of studies on task-based functional connectivity during arithmetic in children**

	Study	N	M_{age}	Age range	Sample	Task	Main findings
1.	Rosenberg-Lee et al. (2011)	45	7.7	7-8	TD	+	↑ connectivity between PFC, parietal, OT and parahippocampal areas in older children
2.	Cho et al. (2012)	86	8.2	7-9	TD	+	↑ connectivity between R-HC and PFC with increasing age and ability level
3.	Qin et al. (2014)	28	8.3	7-9	TD	+	↑HC connectivity with PFC with increasing age
		20	15.61	14-17			HC connectivity with frontal and parietal areas correlates with growth in arithmetic
		20	20.50	19-20			
4.	Rosenberg-Lee et al. (2015)	20	8.44	7-9	TD	+, -	Hyper-connectivity between IPS and PFC in DC
		16	8.34	7-9	DC		
5.	Chang et al. (2016)	25	8.8	7-10	TD	-	Connectivity between left anterior SMG and PFC shows a non-linear association with age
		19	15.7	13-17			
		26	20.6				

Note. DC = dyscalculia.

Table 3**Summary of studies on resting-state functional connectivity and its association with arithmetic in children**

	Study	N	<i>M</i>_{age}	Age range	Sample	Behavioral measures	Main findings
1.	Supekar et al. (2013)	24	8.5	8-9	TD	Gains in on single-digit addition after math tutoring	HC- PFC connectivity at pretest shows positive association intervention gains
2.	Evans et al. (2015)	20	?	7-9	TD	WIAT- Arithmetic	Connectivity between DLPFC, posterior parietal, OT and anterior temporal regions predicts arithmetic ability
3.	Jolles et al. (2016)	19	8.8	7-9	TD		Hyper-connectivity in DC between IPS and other parietal, frontal and occipito-temporal areas,
		19	8.9	7-9	DC		Increased connectivity between left and right IPS in DC, Connectivity patterns differentiate TD and DC
4.	Jolles, Supekar, et al. (2016)	21	8.6	7-9	TD	Gains in on single-digit addition after math tutoring	Intervention increases IPS intrinsic connectivity with PFC, ventral OT and HC. Increases in IPS connectivity were positively correlated with performance gains in the intervention.
		21	9.1	7-9			

Note. DC = dyscalculia. WIAT = Wechsler Individual Achievement Test

Table 4**Summary of DTI studies that correlate white matter structure and arithmetic**

	Study	N	M _{age}	Age range	Sample	Behavioral measures	Main findings
1.	Barnea-Goraly et al. (2005)	19	14.4	7-19	TD	Arithmetic (WISC)	FA of tracts adjacent to SMG, AG and IPS positively correlated with arithmetic
2.	van Eimeren et al. (2008)	13	8.4	7-9	TD	Numerical operations (WIAT) Mathematical reasoning (WIAT)	FA in L-SCR and ILF positively associated with arithmetic
3.	Pavlova et al. (2009)	11	14.6	13-16	PPVL	Mental calculation	No association between connectivity and mental calculation
4.	Rykhlevskaia et al. (2009)	24	8.8	7-9	TD		Lowered FA of ILF and IFOF in DC
		23	8.9	7-9	DC		
5.	Tsang et al. (2009)	25	12.6	10-15	TD	Approximate addition	FA of anterior SLF positively correlated with approximate addition
6.	Lebel et al. (2010)	21	9.2	5-13	FASD	Quantitative concepts (Woodcock Johnson-III)	FA in left parietal SLF positively correlated with math scores
7.	Till et al. (2011)	31	16.4	11-19	MS	Numerical operations (WIAT)	FA in corpus callosum and in right frontal and parietal areas positively correlated with arithmetic ability
8.	Li et al. (2013)	47	10.5	9-11	TD	Arithmetic (WISC)	FA in left SLF and ILF and bilateral IFOF positively correlated with arithmetic
9.	Matejko et al. (2013)	30	18.0	17-18	TD	PSAT	FA in left parietal areas (SLF, superior CR, cortico-spinal tract) positively correlated with math scores
10.	Ranpura et al. (2013)	11	?	8-14	TD		Reduced FA in temporo-parietal areas in DC
		11	?	8-14	DC		
11.	Van Beek et al. (2014)	18	12.0	11-12	TD	Addition, subtraction, multiplication and division	FA of left anterior AF positively correlated with addition and multiplication but not with subtraction and division
12.	Jolles, Wassermann, et al. (2016)	18	?	7-9	TD	Gains in addition and subtraction performance after math tutoring	Changes in left SLF associated with performance gains after tutoring

Note. DC = Dyscalculia. FA = Fractional Anisotropy. FASD = Fetal alcohol spectrum disorder. IFOF = Inferior Frontal-Occipital Fasciculus. MS = multiple sclerosis. PPVL = Prematurely born with periventricular lesions. PSAT = Preliminary Scholastic Achievement Test. TD = Typically developing. VCFS = Velocardiofacial syndrome. WIAT = Wechsler Individual Achievement Test. WISC = Wechsler Intelligence Scale for Children.

Table 5

Summary of structural brain imaging studies that correlate brain structure and arithmetic

	Study	N	M _{Age}	Age range	Sample	Method	Behavioral measure	Main finding
1.	Isaacs et al. (2001)	12 12	15.7 15.8	? ?	VLBW- NC VLBW-C	GMV		Reduced GMV in VLBW-C in L IPS
2.	Rotzer et al. (2008)	12 12	9.7 9.3	? ?	TD DC	GMV WMV		Reduced GMV in DC in IPS, MFG Reduced WMV in DC in Left PFC
3.	Rykhlevskaia et al. (2009)	24 23	? ?	7-9 7-9	TD DC	GMV WMV		Reduced GMV in DC in IPS, FG, HC Reduced WMV in DC in right temporo-parietal cortex
4.	Han et al. (2013)	20 20	10.9 10.8	? ?	LA HA	Anatomical variations		Anatomical differences between LA and HA in OT, orbitofrontal and insular areas
5.	Li et al. (2013)	59	10.5	9-11	TD	GMV	Arithmetic (WISC)	GMV in left IPS positively correlated with arithmetic
6.	Ranpura et al. (2013)	11 11	? ?	8-14 8-14	TD DC	GMV WMV		Reduced GMV in DC in posterior parietal cortex.
7.	Supekar et al. (2013)	24	8.5	8-9	TD	GMV	Single-digit addition after math tutoring	Pre-tutoring GMV in right HC predicts intervention gains
8.	Evans et al. (2015)	43	?	7-9	TD	GMV	Numerical Operations (WIAT)	GMV in posterior parietal areas and ventral OT predict gains in arithmetic
9.	Price et al. (2016)	50	7.4	6-8	TD	GMV	Woodcock Johnson -III Math Composite	GMV in left IPS predicts arithmetic

Note. DC = dyscalculia. GM = Grey Matter Volume. HA = high arithmetic achievement. LA = low arithmetic achievement. VLBW-NC = very low birth weight – no calculation deficits. VLBW-C = very low birth weight – calculation deficits. WIAT = Wechsler Individual Achievement Test. WISC = Wechsler Intelligence Scale for Children. WMV = White Matter Volume.

Figure 1

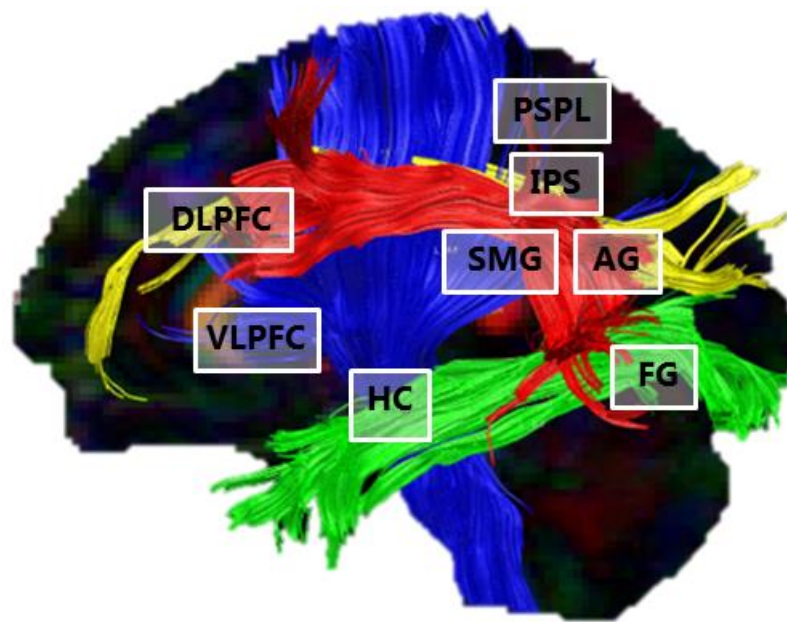


Figure 1. Sagittal slice showing the arithmetic network. The white boxes indicate the most relevant areas implicated in arithmetic, including DLPFC = dorsolateral prefrontal cortex, VLPFC = ventrolateral prefrontal cortex, HC = hippocampus, PSPL = posterior superior parietal lobe, IPS = intraparietal sulcus, SMG = supramarginal gyrus, AG = angular gyrus and FG = fusiform gyrus. The colored tracts represent the most relevant white matter connections as revealed via spherical deconvolution analysis of DTI data. Yellow = Superior longitudinal fasciculus (SLF); Red = Arcuate fasciculus (AF); Blue = Corona radiata (CR); Green = Inferior longitudinal fasciculus (ILF).